Method of Lines Analysis of Soret and Dufour Effects on an Unsteady Heat and Mass Transfer MHD Natural Convection Couette Flow

M. O. Durojaye a*, J. A. Kazeem a, F. O. Ogunfiditimi a and I. J. Ajie b

a Department of Mathematics, University of Abuja, Nigeria.
b Mathematics Programme, National Mathematical Center, Abuja, Nigeria.

Authors’ contributions
This work was carried out in collaboration among all authors. Author MOD designed the study. Author JAK performed the numerical analysis and wrote the first draft of the manuscript. All authors managed the analyses of the study and the literature searches. All authors read and approved the final manuscript.

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ABSTRACT
This study examines the numerical solutions of an unsteady natural convection Couette flow of a viscous, incompressible and electrically conducting fluid between the two vertical parallel plates in the presence of thermal radiation, Soret and Dufour. The fundamental dimensionless governing partial differential equations for the impulsive movement of the plate are solved by method of lines (MOL). The numerical simulations for the effects of Soret and Dufour on the velocity profile, the temperature profile and the concentration profile of the flow are shown graphically. The analysis indicates that the fluid velocity is an increasing function of Soret and Dufour numbers. Also, the concentration profile and the temperature profile increase with increase in the Soret number and Dufour number respectively.

*Corresponding author: E-mail: mayojaye@yahoo.com;
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1. INTRODUCTION

In fluid dynamics, Couette flow refers to the laminar, incompressible, steady flow between two infinitely long parallel plates, top plate moving steadily and sustains the flow, with bottom plate being stationary. Such flow is driven by virtue of viscous drag force acting on fluid and the applied pressure gradient parallel to the plates. Magnetohydrodynamic (MHD) flow between two parallel plates in the presence of a transversely applied magnetic field has several applications in MHD power generators, MHD pumps, accelerators, aerodynamics, heating, electrostatic precipitation, polymer technology, petroleum industry, purification of molten metals from non-metallic inclusions and fluid droplets-sprays, Srinivasa et al. [1].

Double diffusion or heat and mass transfer has numerous applications in engineering processes: exchanger devices, petroleum reservoirs, chemical catalytic reactors and processes, nuclear waste disposal etc. Double diffusive flow is driven by buoyancy due to temperature and concentration gradients. When heat and mass transfer occur together in a fluid flow, the reactions between the energy fluxes induced by the transverse action of both temperature and composition gradients and the driving potentials are more complicated. While the energy flux induced by a composition gradient is termed Dufour or diffusion-thermal effect, the mass fluxes induced by a temperature gradient is termed Soret or thermal-diffusion effect. In general, Dufour and Soret are of smaller order of magnitude than the effects prescribed by Fick’s laws and are often neglected in heat and mass transfer processes by many researchers [2]. The effects of Soret for instance has been utilized for isotope separation, Alao et al. [2]. Hayat et al. [3] had investigated soret and dufour effects on magnetohydrodynamic (MHD) flow of casson fluid. Rao and Viswanatha [4] studied the effects of soret and dufour on hydromagnetic heat and mass transfer over a vertical plate in a porous medium with a convective surface boundary condition and chemical reaction. Bhavena et al. [5] worked on the soret effect on free convective unsteady MHD flow over a vertical plate with heat source.

Many authors had worked on various aspects of heat transfer of Couette flow under the influence of some pertinent physical parameters. Umavathi et al. [6] studied the analytical solution of generalized plain heat transfer of Couette flow in a composite channel. Rajput and Sahu [7] analyzed the effects of thermal radiation and heat source/sink on the natural convection in unsteady hydromagnetic Couette flow of a viscous incompressible electrically conducting fluid confined between two vertical parallel plates with constant heat flux at one boundary. The system of non-linear differential equations of a Newtonian magnetic lubricant squeeze film flow with magnetic induction effects had been solved and analyzed using the combination of the differential transform method and Padé approximation, by Mohammad et al. [8]. Victor and Sreedhara [9] used Galerkin’s finite element method while studying unsteady hydromagnetic natural convection Couette flow through a vertical channel in the presence of thermal radiation under an exponentially decaying pressure gradient with viscous and joule dissipation effects. Seth et al. [10] worked on influence of Hall current on unsteady MHD convective Couette flow of heat absorbing fluid due to accelerated movement of one of the plates of the channel in a porous medium. In Abderrahim et al. [11], the Gear-Chebyshev-Gauss-Lobatto collocation method was used in analysing the unsteady Couette nanofluid flow with heat transfer for copper-water nanofluid under the combined effects of the thermal radiation and a uniform transverse magnetic field with variable thermo-physical properties. Durojaye et al. [12] analysed the effects of some thermo-physical properties of fluid on heat and mass transfer flow past semi-infinite moving vertical plate with viscous dissipation using method of lines. The method of lines analysis of the effects of some flow parameters on unsteady mhd fluid flow past a moving vertical plate embedded in porous medium in the presence of hall current and rotating system, was also studied by Durojaye et al. [13]

In this paper we have used an effective and efficient semi-analytical method with moderate to minimal computational efforts and time when compared with other numerical methods in literatures in examining the effects of thermal diffusion (Soret) and diffusion thermo (Dufour) on an unsteady two-dimensional heat and mass transfer radiative MHD natural convective Couette flow with suction, in a porous medium, under the influence of a uniform transverse magnetic field subject to appropriate boundary conditions. Here, we only consider the case of impulsive movement in the plate and the coupled
nonlinear PDEs governing the flow in dimensionless forms are decoupled and solved using the method of lines (MOL).

2. MATHEMATICAL MODEL AND ANALYSIS

In Fig. 1, we consider two-dimensional unsteady natural convective Couette flow of a viscous, electrically conducting fluid past a vertical porous plate with suction, under the influence of a uniform transverse magnetic field, thermal radiation, heat and mass transfer. The $x$'-axis and $y$'-axis are taken along the plate in the vertical upward and normal direction to the plate respectively. Let the plates be separated by a distance, $h$. At time $t' \leq 0$, the fluid and the plates of the channel are assumed to be at rest and at same temperature $T_h$ and concentration, $C_{0'}$. When the time $t' > 0$, the plate at $y' = 0$ starts moving with time dependent velocity, $U_{0'} t^n$, where $U_0$ is a constant and $n$ is a non-negative integer, in its own plane and at the same time the plate temperature and concentration is raised to $T_{w'}$ and $C_{0'}$ respectively while the plate at $y' = h$ is kept fixed. At the same time $t' > 0$, the wall at $y' = h$ is stationary and maintained at a constant temperature $T_h$ and constant concentration $C_{0'}$. It is assumed that the transverse magnetic field of the uniform strength $H_{0'}$ is to be applied normal to the plate while the Hall Effect, viscous dissipation and induced magnetic field are negligible due to the very small magnetic Reynolds number being considered. Furthermore, it is assumed that the voltage is not applied which implies the absence of an electric field while the homogeneous chemical reaction of first order with rate constant $\beta$ between the diffusion species and the fluid is neglected. In addition, the fluid has constant thermal conductivity and kinematic viscosity. In view of the assumptions above and considering the Boussinesq’s approximation, the governing equations for the flow is given by the following partial differential equations. Srinivasa et al. [1].

Momentum equation:

$$\frac{\partial u'}{\partial t'} = \nu \frac{\partial^2 u'}{\partial y'^2} + \beta (T' - T_h'^0) + \beta (C' - C_h'^0) - \frac{\alpha_{\nu} H_{0'}^2}{\rho} (u' - U_{0'} t^n)$$  

Energy equation

$$\frac{\partial T'}{\partial t'} = \frac{k}{\rho c_p} \frac{\partial^2 T'}{\partial y'^2} + \frac{\nu k T'}{c_{v} c_p} \frac{\partial C'}{\partial y'^2} - \frac{1}{\rho c_p} \frac{\partial q_r}{\partial y'} + \frac{1}{\rho c_p} \frac{\partial q_r}{\partial y'} - \frac{\partial^2 \bar{T} r}{\partial y'^2}$$  

Species diffusion equation:

$$\frac{\partial C'}{\partial t'} = D \frac{\partial^2 C'}{\partial y'^2} + \frac{\nu k T'}{c_{v} c_p} \frac{\partial C'}{\partial y'^2}$$  

The corresponding initial and boundary conditions are:

$$t' \leq 0: u' = 0, T' = T_h'^0, C' = C_h'^0 \text{ for } 0 \leq y' \leq h$$

$$t' > 0: u' = U_{0'} t^n, T' = T_w'^0, C' = C_w'^0 \text{ at } y' = 0$$

$$u' = 0, T' = T_h'^0, C' = C_h'^0 \text{ at } y' = h$$

where $u'$ - velocity component in $x'$-direction, $T'$-temperature of fluid, $C'$-concentration of fluid.

$C_h'$-Concentration susceptibility ($m \text{ mol}^{-1}$), $D_m$-Mass diffusivity ($m^2 s^{-1}$), $k_{r}$-Thermal diffusion ratio, $q_r$-radiative heat flux, $D$-Chemical molecular diffusivity ($m^2 s^{-1}$), $T_m$-Mean fluid temperature ($K$), $\beta$-Thermal diffusion ratio, $\beta_0$-Catalytic constant, $\beta_1$-Thermal conductivity of the fluid ($W m^{-1} K^{-1}$), $C_p$-Specific heat at constant pressure ($J kg^{-1} K^{-1}$), $\alpha_{\nu}$-Magnetic Reynolds number.

The radiative heat flux in equation (2) is simplified by making use of the Rosseland approximation, Adegbie and Fagbade [14]:

$$q_r = -\frac{4\bar{\sigma}}{3k'} \frac{\partial \bar{T} r}{\partial y'}$$  

where $\bar{\sigma}$ - Stefan–Boltzmann constant ($W m^{-2} K^{-4}$), $k'$ - mean absorption coefficient ($m^{-1}$).
Following Rajput and Sahu [7], we assume that the differences in temperature within the flow are sufficiently small such that \( q_r \) is expressed as a linear function of \( T^k \). Hence on expanding \( T^k \) in a Taylor Series about \( T_h^k \) up to first order approximation, we have:

\[
T^k \approx T_h^k + 4(T^k - T_h^k) T_h^k = 4T^k - 3T_h^k^2
\]  

(6)

Using equations (5) and (6) in the last term of equation (2), we obtain:

\[
\frac{\partial q_r}{\partial y} = -\frac{16\alpha q_h^3}{3k^2} \frac{\partial T^k}{\partial y^2}
\]

(7)

Substituting equation (7) in the equation (2), the energy equation becomes:

\[
\frac{\partial T}{\partial t} = \frac{k}{\rho c_p y^2} \frac{\partial T^k}{\partial y^2} + \frac{\partial^2 q_r}{\partial y^2}
\]

(8)

To transform the governing equations and boundary conditions into dimensionless form, the following non-dimensional quantities are introduced. Srinivasa et al. [1]

\[
u = \frac{u}{h}, \quad \theta = \frac{T - T_h^k}{T_w - T_h^k}, \quad \phi = \frac{c_v - c_w}{c_v - c_h},
\]

\[G_r = \frac{\beta \rho h (T_w - T_h^k)}{\nu}, \quad \theta = \frac{T - T_h^k}{T_w - T_h^k}, \quad \phi = \frac{c_v - c_w}{c_v - c_h},
\]

\[
G_c = \frac{\beta \rho h (C_v - C_h) \nu}{F}, \quad F = \frac{\alpha^2 h^2}{\nu}, \quad M^2 = \frac{\alpha^2 h^2}{\nu}, \quad R = \frac{3k^2}{\alpha^2 h^2}, \quad D_r = \frac{\alpha h}{\nu}, \quad S_r = \frac{\alpha h}{\nu}
\]

(9)

In view of non-dimensional quantities in equation (9), the equations (1), (3) and (8) reduce to the following non-dimensional form:

\[
\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial y^2} + G_r \theta + G_c \phi - M^2 (u - F t^m)
\]

(10)

\[
\frac{\partial \theta}{\partial t} = \frac{1}{Pr} \left( \frac{3k^2}{3R} \right) \frac{\partial^2 \theta}{\partial y^2} + D_r \frac{\partial^2 \phi}{\partial y^2}
\]

(11)

\[
\frac{\partial \phi}{\partial t} = \frac{1}{Sc} \frac{\partial^2 \phi}{\partial y^2} + S_c \frac{\partial^2 \theta}{\partial y^2}
\]

(12)

Similarly, using equation (9), the initial and boundary conditions in equation (4) reduce to:

\[
t < 0: u = 0, \quad \theta = 0, \quad \phi = 0 \quad \text{for} \quad 0 \leq y \leq 1
\]

(13)

\[
t > 0: u = F t^m, \quad \theta = 1, \quad \phi = 1 \quad \text{at} \quad y = 0
\]

\[
u = 0, \quad \theta = 0, \quad \phi = 0 \quad \text{at} \quad y = 1
\]

Considering the impulsive movement of the plate at \( y = 0 \) i.e. \( v = 0 \), equation (10) becomes:

\[
\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial y^2} + G_r \theta + G_c \phi - M^2 (u - F)
\]

(14)

and the corresponding initial and boundary conditions (13) become:

\[
t < 0: u = 0, \quad \theta = 0, \quad \phi = 0 \quad \text{for} \quad 0 \leq y \leq 1
\]

\[
t > 0: u = F, \quad \theta = 1, \quad \phi = 1 \quad \text{at} \quad y = 0
\]

\[
u = 0, \quad \theta = 0, \quad \phi = 0 \quad \text{at} \quad y = 1
\]

where \( G_r \) - Grashof number for heat transfer, \( G_c \) - Grashof number for mass transfer, \( M \) - Hartmann number, \( P_r \) - Prandtl number, \( S_c \) - Schmidt number, \( F \) - Accelerating parameter, \( R \) - Thermal radiation parameter, \( S_r \) - Soret number, \( D_r \) - Dufour number, \( u \) - velocity of the fluid, \( \theta \) - temperature of the fluid, \( \phi \) - concentration of the fluid, \( t \) - time in dimensionless forms, Srinivasa et al. [1].
The skin-friction or the shear stress at the moving plate of the channel in non-dimensional form is given by:

$$\tau = -\left(\frac{\gamma_w}{\rho u_0}\right)_{y=0} = -\left(\frac{\partial u}{\partial y}\right)_{y=0} \quad (16)$$

The rate of heat transfer at the moving hot plate of the channel in non-dimensional form is given by:

$$Nu_0 = -x\left(\frac{\partial^2 T}{\partial y^2}\right)_{y=0}, \quad Nu_0 Re_x^{-1} = -\left(\frac{\partial \theta}{\partial y}\right)_{y=0} \quad (17)$$

The rate of heat transfer on the stationary plate is given by:

$$Nu_1 = -x\left(\frac{\partial^2 T}{\partial y^2}\right)_{y=0}, \quad Nu_1 Re_x^{-1} = -\left(\frac{\partial \theta}{\partial y}\right)_{y=1} \quad (18)$$

The Sherwood number at the moving plate of the channel in non-dimensional form is given by:

$$Sh = -x\left(\frac{\partial^2 C}{\partial y^2}\right)_{y=0}, \quad Sh Re_x^{-1} = -\left(\frac{\partial \phi}{\partial y}\right)_{y=0} \quad (19)$$

where $Re_x$ is the Reynold's number. Srinivasa et al. [1]

3. METHOD OF LINES (MOL)

Method of Lines as a numerical procedure for solving partial differential equations (PDE's) had been reported to give accurate approximate solutions, and its successful application to new PDE problems depends on the experience and cleverness of the analyst. Instead of being a unique, direct and clearly defined approach, MOL is a general concept that requires specific details of each new PDE problem. The main idea of the MOL is to replace the spatial (boundary value) derivatives in the partial differential equations (PDE’s) with algebraic approximations. With this, only the initial value variable, typically time in a physical problem, remains and thus we have a system of ordinary differential equations (ODE’s) that approximates the given partial differential equations. Putting stiffness of the system of ODE’s generated into consideration, an appropriate integration algorithm for initial value ODE’s is chosen for numerical computations. As a result, we obtain approximate solutions to the given PDE’s. Griffiths and Schiesser [15,16,17], Schiesser [18], Knapp [19], Biazar and Nomidi [20].

Linearizing and explicitly decoupling equations (11), (12) and (14), the following approximations are adopted: $\frac{\partial \phi}{\partial y} \approx 1$ in equation (11), $\frac{\partial^2 \theta}{\partial y^2} \approx 1$ in equation (12), $\theta \approx 1$,

$\phi \approx 1$ in equation (14). Chung [21]. Considering the adopted approximations, equations (11), (12), (14), are rewritten as:

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial y^2} + G_r + G_c - M^2(U - F) \quad (20)$$

$$\frac{\partial \theta}{\partial t} = \frac{1}{Fr} \left(\frac{3R+4}{3h^2}\right) \frac{\partial^2 \theta}{\partial y^2} + D_r \quad (21)$$

$$\frac{\partial \phi}{\partial t} = \frac{1}{Sc} \frac{\partial^2 \phi}{\partial y^2} + S_r \quad (22)$$

Then, we solve equations (20) – (22) subject to the transformed boundary conditions (15) by Method of Lines (MOL). Discretizing equation (20) in space variable $y$ while leaving time variable $t$ continuous, we have the system of ODE’s:

$$\left(\frac{du}{dt}\right)_i = \frac{u_{i+1} - 2u_i + u_{i-1}}{h^2} + G_r + G_c - M^2 u_i + M^2 F \quad (23)$$

$$= \frac{1}{h^2} u_{i-1} - \left(\frac{2}{h^2} + M^2\right) u_i + \frac{1}{h^2} u_{i+1} + G_r + G_c + M^2 F$$

$$= a_1 u_{i-1} - a_2 u_i + a_3 u_{i+1} + a_4 \quad (24)$$

where, $a_1 = a_3 = \frac{1}{h^2}, \quad a_2 = \frac{2}{h^2} + M^2, \quad a_4 = G_r + G_c + M^2 F \quad (25)$

Now, equations (24) – (25) with boundary conditions $u(0,t) = u_0(y,t) = F$ and $u(N + 1, t) = u(0, t) = 0$, can be solved iteratively. For $i=1, 2, ..., N, \quad u(0,t) = u_0(y,t) = F$, and $u(N + 1, t) = u(1, t) = 0$, equation (24) can be written in matrix form:

$$\begin{pmatrix}
\frac{du}{dt}
\end{pmatrix}_i = \begin{pmatrix}
a_1 & a_2 & 0 & 0 & ... & 0 & 0
0 & a_1 & a_2 & 0 & ... & 0 & 0
0 & 0 & a_1 & a_2 & ... & 0 & 0
0 & 0 & 0 & a_1 & a_2 & ... & 0
0 & 0 & 0 & 0 & a_1 & a_2 & ... \\
\end{pmatrix} \begin{pmatrix}
u_i
\end{pmatrix} + \begin{pmatrix}
F
u_{i-1}
u_1
\end{pmatrix} \quad (26)$$

where the coefficients $a_1, a_2, a_3$ and $a_4$ are given by equation (25) and $\frac{du}{dt} = \left(\frac{d\phi}{dt}\right)_i$

In the same way, equation (21) becomes:

$$\left(\frac{d\theta}{dt}\right)_i = \frac{3R+4}{3h^2Fr} \left(\frac{\phi_{i+1} - 2\phi_i + \phi_{i-1}}{h^2}\right) + D_r \quad (27)$$

$$= \frac{3R+4}{3h^2Fr} \theta_{i-1} - 2 \left(\frac{3R+4}{3h^2Fr}\right) \theta_i + \frac{3R+4}{3h^2Fr} \theta_{i+1} + D_r$$
Now, equations (28) – (29) with conditions \( \theta(0, t) = \theta_0(y, t) = 1 \) and \( \theta(N + 1, t) \approx \theta(1, t) = 0 \) can be solved iteratively. For \( i = 1, 2, \ldots, N \), \( \theta(0, t) = \theta_0(y, t) = 1 \) and \( \theta(N + 1, t) \approx \theta(1, t) = 0 \), equation (28) can be written in matrix form:

\[
\begin{bmatrix}
\dot{\theta}_1 \\
\dot{\theta}_2 \\
\vdots \\
\dot{\theta}_{N-1} \\
\dot{\theta}_N
\end{bmatrix}
=
\begin{bmatrix}
\beta_1 & \beta_2 & 0 & \cdots & 0 \\
0 & \beta_1 & \beta_2 & \cdots & 0 \\
\vdots & \vdots & \ddots & \ddots & \vdots \\
0 & 0 & 0 & \cdots & \beta_1 \\
0 & 0 & 0 & \cdots & \beta_2 \\
\end{bmatrix}
\begin{bmatrix}
\theta_1 \\
\theta_2 \\
\vdots \\
\theta_{N-1} \\
\theta_N
\end{bmatrix}
+ \begin{bmatrix}
\beta_4 \\
\vdots \\
\vdots \\
\beta_4
\end{bmatrix}
\tag{30}
\]

where the coefficients \( \beta_1, \beta_2, \beta_3 \) and \( \beta_4 \) are given by equation (29) and \( \dot{\theta}_i = \left( \frac{d\theta}{dt} \right)_i \).

Similarly, equation (22) becomes:

\[
\left( \frac{d\phi}{dt} \right)_i = \frac{1}{Sc} \phi_{i+1} + \frac{E_f}{h^2} \phi_i + \frac{1}{Sc} \phi_{i+1} + S_r
\tag{31}
\]

\[
= \frac{1}{h^2 Sc} \phi_{i-1} - \frac{2}{h^2 Sc} \phi_i + \frac{1}{h^2 Sc} \phi_{i+1} + S_r
= \gamma_1 \phi_{i-1} - \gamma_2 \phi_i + \gamma_3 \phi_{i+1} + \gamma_4
\tag{32}
\]

Where

\[
\gamma_1 = \frac{1}{h^2 Sc}, \quad \gamma_2 = \frac{-2}{h^2 Sc}, \quad \gamma_3 = \frac{1}{h^2 Sc}, \quad \gamma_4 = S_r \tag{33}
\]

\( \phi(N + 1, t) = \phi(1, t) = 0 \), can be solved iteratively. For \( i = 1, 2, \ldots, N \), \( \phi(0, t) = \phi_0(y, t) = 1 \) and \( \phi(N + 1, t) \approx \phi(1, t) = 0 \), equation (32) can be written in matrix form:

\[
\begin{bmatrix}
\phi_1 \\
\phi_2 \\
\vdots \\
\phi_{N-1} \\
\phi_N
\end{bmatrix}
= \begin{bmatrix}
\gamma_1 & \gamma_2 & 0 & \cdots & 0 \\
0 & \gamma_1 & \gamma_2 & \cdots & 0 \\
\vdots & \vdots & \ddots & \ddots & \vdots \\
0 & 0 & 0 & \cdots & \gamma_1 \\
0 & 0 & 0 & \cdots & \gamma_2 \\
\end{bmatrix}
\begin{bmatrix}
\phi_1 \\
\phi_2 \\
\vdots \\
\phi_{N-1} \\
\phi_N
\end{bmatrix}
+ \begin{bmatrix}
\gamma_3 \\
\vdots \\
\vdots \\
\gamma_3
\end{bmatrix}
\tag{34}
\]

where the coefficients \( \gamma_1, \gamma_2, \gamma_3 \) and \( \gamma_4 \) are given by equation (33) and \( \phi_i = \left( \frac{d\phi}{dt} \right)_i \).

4. RESULTS AND DISCUSSION

This paper examines the effects of Soret and Dufour on an unsteady two-dimensional heat and mass transfer radiative MHD natural convective Couette flow of a viscous, incompressible, electrically conducting fluid between the two vertical parallel plates with suction, in a porous medium, and subject to a uniform transverse magnetic field. In the analysis, method of lines (MOL) is used to solve the dimensionless forms of the governing equations of the fluid flow. Unless otherwise stated, the values: \( G_r = 5.0, G_c = 5.0, \quad \xi = 2.0, \quad h = 0.1, \quad Pr = 0.71, \quad D_f = 1, \quad Sc = 0.22, \quad Sr = 1, \quad R = 2.0, \quad F = 0.5 \), for the flow parameters, are used in MATLAB codes for the computations and graphical simulations. Fig. 2 and Fig. 4, respectively, show the effects of variations in Dufour number on velocity distribution and temperature distribution of the flow. The Dufour number establishes the contribution of concentration gradients to the thermal energy flux of the flow. As Dufour number increases, both the velocity and the temperature profiles of the flow increase. Also, Fig. 3 and Fig. 5, respectively, show the effects of variations in Soret number on velocity distribution and concentration distribution of the flow. The Soret number signifies the effect of the temperature gradients causing significant mass diffusion effects. As Soret number increases, the velocity profile as well as the concentration profile of the flow increases.
Fig. 3. Velocity profile with variations in Soret Number ($S_T$)

Fig. 4. Temperature profile with variations in Dufour Number ($D_T$)

Fig. 5. Concentration profile with variations in Soret Number ($S_T$)
5. CONCLUSION

In this paper, we use method of lines (MOL) in solving the governing equations of the fluid flow in dimensionless forms, and also in analyzing the effects of Dufour and Soret on velocity profile, temperature profile and concentrations profile of the flow. The results from the study show that:

- Increase in Dufour and Soret number causes increase in the velocity profile of the flow.
- Increase in Dufour number causes increase in the temperature profile of the flow.
- Increase in Soret number causes increase in the concentration profile of the flow.
- The interpretations of the graphical simulations in Fig. 2 - Fig. 5, of the present study agrees with those of previous study by Srinivasa et.al [1].

COMPETING INTERESTS

Authors have declared that no competing interests exist.

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